

# Convergence to market efficiency of top losers

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## Abstract

We use top losers to examine convergence speed of order imbalance on stock return since order imbalance has been claimed to be a state variable in cross sectional return. We found that significance of order imbalance coefficients decreased with increasing time interval (5, 10 and 15-min), indicating evidences on convergence to market efficiency. We also employ a time varying GARCH model to examine the relation between order imbalance and volatility. Again, the significance of order imbalance coefficients shows a decay pattern which also supports convergence to market efficiency hypothesis. We suspect that small firm effect plays a role in convergence. However, our empirical results do not suggest an expected negative relation between order imbalance coefficients and market capitalization.

Finally, we developed an imbalance-based trading strategy and made profit from these daily top losers. We short sell seller-initiated order imbalances and buy back buyer-initiated order imbalances. We try many scenarios in testing our strategy. All of them outperformed buy and hold strategy. In order to explain the profitability of order imbalance based strategy, we examine the causal relationship between return and order imbalance. We find that order imbalance is a good indicator of price discovery under our nested causality framework.

***Key word: market efficiency, order imbalance, top losers.***

## **1. Introduction**

Market efficiency has drawn much attention in finance field, which was defined by Fama (1970). Market efficiency suggests that at any given time, prices fully reflect all available information on a particular stock or market. Following this concept, no investor has a privilege in predicting return because no one has access to information not already available to everyone else. However, researchers have compiled a long list of empirical anomalies in the real world.

For decades, price movement is a central issue for many scholars, and much research has been devoted to finding the relation between return and trading volume. Recently, Chordia et al. (2002) documented a seemingly related and intriguing phenomenon in their study of market-wide order imbalances on the New York Stock Exchange. The market order imbalance, define as aggregated daily market purchase orders less sell order for stocks in the S&P500 index, is highly predictable from day-to-day. A day with a high imbalance on the buy side will likely be followed by several additional days of aggregate buy-side imbalances; and similarly for an initial imbalance on the sell side. This implies that investors continue buying or selling for quite a long time, either because they are herding, or because they are splitting large orders across days, or both. In addition, Chordia et al. (2004) studied on the relation between order imbalance and daily returns of individual stocks. Price pressures caused by auto-correlated imbalances cause a positive relation between lagged imbalances and returns, which reverses sign after controlling for the current imbalance.

The major purpose of this study is to examine the convergence to market efficiency of top losers, which incorporate important private or public information within intraday trading. We would like to examine whether order imbalance has a significant influence on return of top losers. In addition, we are curious about how

long it takes for market efficiency. Therefore, we investigate three time intervals (5-, 10-, and 15-min) recommended by Chordia during daily price formation process.

We first examine both contemporaneous and lagged relations between returns and order imbalances. The empirical results show that lagged imbalances are positively related to returns. In particular, about 77% of the coefficients on the first lag of order imbalances are positive, and more than a quarter are positive and significant. Our empirical results also indicated that the current imbalances are positive and significant for virtually all the firms. The contemporaneous relation between imbalances and returns is consistent with both inventory and asymmetric information effects of price formation.

We then use a time varying GARCH (1,1) model to investigate the relation between volatilities and order imbalances. We expected a positive order imbalance accompanied by a large volatility on stock price. The empirical results show that about half of significant coefficients are positively associated between volatility and order imbalance. We have two stories to explain the finding. 1) The evidence implies that market makers have good ability to control the volatility of stock price, and using the bid-ask spread to adjust the stock price fluctuation in the market. 2) Market makers pay their attention on the “stability of the market” more than on the “rate of return”.

Moreover, our empirical finds show a clear pattern on convergence to market efficiency. We document a declining trend of the significant coefficients in longer time interval. The results suggest that the order imbalance still have strong influence on volatility in the short time, while market makers reduce the influence in longer period of time. Fourth, we test whether there is a small firm effect in return-order imbalance relation. We expected to see a negative sign between order imbalance coefficients and market capitalizations. If the relation was significant, we conclude

that small caps are easily to be manipulated.

Finally, we manage to develop an imbalance-based trading strategy for top losers. In order to tell a story behind the profitability of order imbalance based trading strategy, our empirical findings indicate that the unidirectional relationship from order imbalances to returns is 13.04% in the small firm size quartile, while the corresponding number is 17.39% in the large firm size quartile during the entire sample period. The size-stratified results can be explained as follows. When the firm size is larger, the percentage of firms exhibiting a unidirectional relationship from order imbalances to returns is higher, indicating that order imbalance is a better indicator for predicting returns in large firm size quartile.

The rest of this study is organized as follow. Section 2 is data and section 3 is methodology. Our empirical results are shown in section 4. Section 5 concludes.

## **2. Data**

Since we already know that serial dependence in return is close to zero for active stock over a daily horizon, our investigation of the efficiency-creating process focus on intra-day trading. Data sources were from the Center for Research in Security Prices (CRSP) and the NYSE Trades and Automated Quotations (TAQ) databases. First, we screen daily return to find daily top losers from July, 2006 to December, 2006. The definition of top loser in this study is the stock which had the worst daily open-to-close return (closing price minus opening price divided by opening price). We collected seventy stocks in our sample. Then, we collected the corresponding intraday data in TAQ database for these 70 samples. Following Lee and Ready (1991), any quote less than five seconds prior to the trade was ignored and the first one at least five seconds prior to the trade was retained. If a transaction occurs above the prevailing quote mid-point, it is regarded as a buyer-initiated order and vice

versa. If a transaction occurs exactly at the mid-point, it is signed from tick test.

In Table 1, the basic information of our 70 sample stocks are presented. Panel A of Table 1 presents the basic statistics including mean, median, standard deviation, skewness, and kurtosis. The mean value of market capitalization is 135 million, and the median is 48 million. The average trading volume is 5,311 thousand, and the median is 1,524 thousand. As shown in Table 1, both the market capitalization and the trading volume have outliers. It self-explains that medians are much smaller than means, and both of them are positive skew. In addition, the mean value of the daily return is -28.53% in our 70 samples. The distribution of market capitalization is demonstrated in Panel B of Table 1. We find that 60% of market capitalizations are under 100 million.

### **3. Methodology**

We employed two different approaches to examine return-order imbalance and volatility-order imbalance. First of all, we examine whether lagged order imbalances have predictability for current stock return. We expected a positive return-lagged imbalance. Since market makers are risk averse, an imbalance creates price pressure from inventory change. However, since liquidity demands are auto-correlated, there is further price pressure at date 2 that is correlated with the date 1 price pressure. This leads to a positive predictive relation between lagged imbalance and future price movements. In addition, if the relations were significant, we could develop a trading strategy.

Furthermore, we included the contemporaneous imbalance and four lags of order imbalance. Conditional of knowing current imbalance, we investigate current return and lagged order imbalance relation. We expected a positive coefficient of current imbalances and negative signs in return-lagged imbalances relations, after

controlling current imbalance.

In order to make sure that return-order imbalance relation from regression is not from associated risk increase, we employ a time varying GARCH (1,1) model to examine time varying return-order imbalance.

$$R_t = \alpha + \beta \times OI_t + \varepsilon_t \quad \varepsilon_t \mid \Omega_{t-1} \sim N(0, h_t) \quad (3)$$

$$h_t = A_1 + B_1 h_{t-1} + C_1 \varepsilon_{t-1}^2$$

where  $R_t$  is the return in period  $t$ , defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_t$  is the explanatory variable, order imbalance

$\beta$  is the coefficient of the impact of order imbalance on stock returns

$\varepsilon_t$  means the residual of the stock return in period  $t$

$h_t$  is the conditional variance in the period  $t$

$\Omega_{t-1}$  is the information set in period  $t-1$

The  $\beta$  coefficient represents whether the order imbalance volumes have significant influence on the stock returns. We are also interested in examining dynamic relation between volatility and order imbalance. Intuitively, we expected that high order imbalances are accompanied by large volatilities.

$$R_t = \alpha + \varepsilon_t \quad \varepsilon_t \mid \Omega_{t-1} \sim N(0, h_t) \quad (4)$$

$$h_t = A_1 + B_1 h_{t-1} + C_1 \varepsilon_{t-1}^2 + D_1 OI_t$$

where  $R_t$  is the return in period  $t$ , defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_t$  is the explanatory variable, order imbalance

$\varepsilon_t$  means the residual of the stock return in period  $t$

$h_t$  is the conditional variance in the period  $t$

$\Omega_{t-1}$  is the information set in period  $t-1$

Based on, Lorente, Michaely, Sarr and Wang (2002), market capitalization is a proxy of information asymmetry. A negative sign is expected from order imbalance coefficient and market cap because small firms are associated with higher information

asymmetry.

In order to explain the story behind order imbalance based trading strategy developed from our empirical results, we employ a nested causality approach to explore the dynamic causal relation between return and order imbalance. According to Chen and Wu (1999), we define four relationship between two random variables,  $x_1$  and  $x_2$ , in terms of constraints on the conditional variances of  $x_{1(T+1)}$  and  $x_{2(T+1)}$  based on various available information sets, where  $x_i = (x_{i1}, x_{i2}, \dots, x_{iT})$ ,  $i=1, 2$ , are vectors of observations up to time period  $T$ .

*Definition 1: Independency,  $x_1 \wedge x_2$  :*

$x_1$  and  $x_2$  are independent if

$$Var(x_{1(T+1)} | \tilde{x}_1) = Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2) = Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2, \tilde{x}_{2(T+1)}) \quad (7)$$

and

$$Var(x_{2(T+1)} | \tilde{x}_2) = Var(x_{2(T+1)} | \tilde{x}_1, \tilde{x}_2) = Var(x_{2(T+1)} | \tilde{x}_1, \tilde{x}_2, \tilde{x}_{1(T+1)}) \quad (8)$$

*Definition 2: Contemporaneous relationship,  $x_1 \langle - \rangle x_2$  :*

$x_1$  and  $x_2$  are contemporaneously related if

$$Var(x_{1(T+1)} | \tilde{x}_1) = Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2) \quad (9)$$

$$Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2) > Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2, \tilde{x}_{2(T+1)}) \quad (10)$$

and

$$Var(x_{2(T+1)} | \tilde{x}_2) = Var(x_{2(T+1)} | \tilde{x}_1, \tilde{x}_2) \quad (11)$$

$$Var(x_{2(T+1)} | \tilde{x}_1, \tilde{x}_2) > Var(x_{2(T+1)} | \tilde{x}_1, \tilde{x}_2, \tilde{x}_{1(T+1)}) \quad (12)$$

*Definition 3: Unidirectional relationship,  $x_1 \Rightarrow x_2$  :*

There is a unidirectional relationship from  $x_1$  to  $x_2$  if

$$Var(x_{1(T+1)} | \tilde{x}_1) = Var(x_{1(T+1)} | \tilde{x}_1, \tilde{x}_2) \quad (13)$$

and

$$\text{Var}(x_{2(T+1)} \Big|_{\sim} x_2) > \text{Var}(x_{2(T+1)} \Big|_{\sim} x_1, x_2) \quad (14)$$

*Definition 4: Feedback relationship,  $x_1 \leq \Rightarrow x_2$  :*

There is a feedback relationship between  $x_1$  and  $x_2$  if

$$\text{Var}(x_{1(T+1)} \Big|_{\sim} x_1) > \text{Var}(x_{1(T+1)} \Big|_{\sim} x_1, x_2) \quad (15)$$

and

$$\text{Var}(x_{2(T+1)} \Big|_{\sim} x_2) > \text{Var}(x_{2(T+1)} \Big|_{\sim} x_1, x_2) \quad (16)$$

To explore the dynamic relationship of a bi-variate system, we form the five statistical hypotheses in the Table 2 where the necessary and sufficient conditions corresponding to each hypothesis are given in terms of constraints on the parameter values of the VAR model.

To determine a specific causal relationship, we use a systematic multiple hypotheses testing method. Unlike the traditional pair-wise hypothesis testing, this testing method avoids the potential bias induced by restricting the causal relationship to a single alternative hypothesis. To implement this method, we employ results of several pair-wise hypothesis tests. For instance, in order to conclude that  $x_1 \Rightarrow x_2$ , we need to establish that  $x_1 \not\Leftarrow x_2$  and to reject that  $x_1 \not\Rightarrow x_2$ . To conclude that  $x_1 \leq \Rightarrow x_2$ , we need to establish that  $x_1 \not\Leftarrow x_2$  as well as  $x_1 \not\Rightarrow x_2$  and also to reject  $x_1 \wedge x_2$ . In other words, it is necessary to examine all five hypotheses in a systematic way before we draw a conclusion of dynamic relationship. The following presents an inference procedure that starts from a pair of the most general alternative hypotheses.

Our inference procedure for exploring dynamic relationship is based on the principle that a hypothesis should not be rejected unless there is sufficient evidence against it. In the causality literature, most tests intend to discriminate between independency and an alternative hypothesis. The primary purpose of the literature

cited above is to reject the independency hypothesis. On the contrary, we intend to identify the nature of the relationship between two financial series. The procedure consists of four testing sequences, which implement a total of six tests (denoted as (a) to (f)), where each test examines a pair of hypotheses.

The four testing sequences and six tests are summarized in a decision-tree flow chart in Table 3. The inference procedure starts from executing tests (a) and (b), which result in one of the four possible outcomes,  $E_1, \dots, \text{ or } E_4$ . The three outcomes,  $E_1, E_2$ , and  $E_3$ , that lead to the conclusions of  $x_1 \leq x_2$ ,  $x_1 = x_2$ , and  $x_1 < x_2$ , respectively, will stop the procedure at the end of the first step. Nonetheless, when outcome  $E_4$  is realized, tests (c) and (d) will be implemented. There again one of the four possible outcomes,  $E_5, \dots, \text{ or } E_8$ , will be realized. The realization of outcomes  $E_5$  and  $E_6$ , which respectively indicates  $x_1 \leq x_2$ , and  $x_1 = x_2$ , will stop the procedure at the end of Step 2. On the other hand, the realization of outcome  $E_7$  would lead to test (e) in Step 3, which has the consequence of either outcome  $E_9$  or outcome  $E_{10}$ . Outcome  $E_9$  implies  $x_1 \leq x_2$  and the procedure will stop. Either outcome  $E_8$  from Step 2 or outcome  $E_{10}$  from Step 3 will lead to test (f) in Step 4. This last step may generate two possible results,  $E_{11}$  and  $E_{12}$ , which imply  $x_1 < - > x_2$  and  $x_1 \wedge x_2$ , respectively.

## 4. Empirical results

### 4.1 Unconditional lagged return-order imbalance relation

Table 4 represents the results of relation between returns and lagged order imbalances, in terms of three time intervals-5, 10 and 15 minutes. The percentages of significantly positive coefficients on the first lag order imbalances are 11%, 9%, and 9% in 5, 10, and 15 minutes respectively, which are larger than the percentages of negative and significant coefficients, 7%, 9%, and 6% in 5, 10, and 15 minutes, respectively. These results are in accordance with daily findings in Chordia and Subrahmanyam (2004). In particular, about 77% of the coefficients on the first lag of

order imbalances are positive, and more than a quarter are significantly positive.

However, our significant test results are inconsistent with their findings. The possible reason is either that our intraday time interval is too short to reveal information timely or that the market is efficient enough to reflect all information. We believe that market makers do not have great price pressures in handling top losers. Apparently, liquidity traders are eager to dump their holdings to market makers.

In convergence speed, we find that percentage of significantly positive at short time interval is much larger than those at long time intervals in Panel B. Our results are consistent with the findings of Chordia et al. (2005). Obviously, at three significant levels, order imbalances have the declining predictive ability on returns as the time interval increases.

#### **4.2 Conditional contemporaneous return–order imbalance relation**

Table 5 represents the results of significant test between contemporaneous returns and order imbalances, in terms of three time intervals-5, 10 and 15 minutes respectively. Coefficients of current return and the contemporaneous order imbalance are 63%, 47%, and 41% positive and significant in 5 minutes, 10 minutes, and 15 minutes respectively. These results are also consistent with the findings of Chordia and Subrahmanyam (2004). The contemporaneous relation between imbalances and returns is consistent with both inventory and asymmetric information effects of price formation.

In convergence, a decreasing trend, 63%, 47%, and 41% in 5, 10, and 15 minutes respectively, has been shown. It implies that the relation between current return and order imbalance is more obvious in short reactive time than in longer time intervals. Furthermore, Chordia and Subrahmanyam (2004) also mentioned that after controlling for the current imbalance, lagged imbalances are negatively related to current price movements. They argued that predictability of lagged imbalance on

future return disappears after controlling for the current order imbalance. However, our empirical results show a different picture. Table 5 shows that percentage in negative and significant coefficients of lagged 1 period imbalances are only 9%, 9%, and 13% in 5, 10, and 15 minutes respectively. A possible explanation is that coefficient on the lagged imbalance reverse sign in the presence of the contemporaneous imbalance only when imbalances are auto-correlated.

#### **4.3 Dynamic relation between order imbalance and return**

Table 6 summarizes the results of dynamic return-order imbalance relation. It shows that positive coefficients of contemporaneous return and order imbalance for 5, 10 and 15 min horizons are 66%, 63% and 64% respectively; those with positive and significant coefficients for 5, 10 and 15-min time intervals are 46%, 40% and 21% respectively at 5% significant level. It implies that order imbalance is an explanatory variable for stock return even in a time varying model. Again, a declining trend in the percentage of significantly positive coefficients implies that market becomes more efficient in longer horizons.

#### **4.4 Dynamic relation between order imbalance and volatility**

We are also interested in examining the relations between volatilities and order imbalances and the expected sign is positive. The empirical results are exhibited in Table 7. The significant coefficients in total samples are 24%, 12%, and 8% in 5-, 10-, and 15-min intervals respectively at the 5% significant level. Meanwhile, about half of those significant coefficients are positive relations between volatilities and order imbalances. The evidence implies that market makers have good ability to control the volatility of stock price, and using the bid-ask spread to adjust the stock price fluctuation in the market.

Moreover, table 7 also demonstrates a clear pattern on convergence to market

efficiency. A declining trend of the significant coefficients in longer time interval is found. The results suggest that the order imbalance still have strong influence on volatility in the short time, while market makers try to reduce it.

#### **4.5 Small firm effect**

It is plausible that inventory pressures induced by order imbalances could differentially affect the return among stocks for different market capitalizations. We expected a significant negative relation between market capitalizations and order imbalances, namely a small firm effect.

In Chordia et al. (2005), they argued that imbalances in larger stocks are offset more efficaciously by market makers, so that predictability of imbalances is removed sooner. Their empirical results showed that the magnitudes of the coefficients are smaller for larger firms, supporting the notion mentioned above that the market for larger stocks is more efficient. In addition, the coefficients continue to decrease with the time interval, which means that the market becomes efficient in longer horizon.

In Panel A of Table 8, the contemporaneous order imbalance – return coefficients from GARCH method were used to examine small firm effect, while the coefficients used in Panel B of Table 8 were collected from OLS. We find that in Panel A and Panel B of Table 8, all the coefficients are insignificant.

#### **4.6 Trading strategy based on return-order imbalance relation**

Given the evidence of the return predictability from order imbalances in previous sections, we try to develop an order imbalance based trading strategy. Average return from buy-and-hold of our 70 top losers is -28.53%. We formed our imbalance-based trading strategy: 1). Short sell when negative order imbalance appears and 2). Buy back when positive order imbalance. We ignore transaction costs and taxes. This trading strategy is based on 2 scenarios – no truncation and 90%

truncation.

The trading results are exhibited in Table 9. In Panel A, we use trading prices. Mean of no truncated return are 9.16%, 9.9%, and 10.35% in 5-, 10-, 15-min respectively. Average return of 90% truncation are 5.86%, 1.14%, and 4.14% in 5-, 10-, 15-min respectively. It implies that our order imbalance based trading strategy beats return of buy and hold. In Panel B of Table 9, the rates of return were calculated by buying stocks at ask price and selling stocks at bid price. We find that all returns of strategies in Panel B are smaller than those in Panel A. In Panel B, mean of no truncated return are -24.91%, -9.93%, and -6.57% in 5-, 10-, 15-min respectively. Average return of 90% truncation are -1.3%, -5.04%, and -6.47% in 5-, 10-, 15-min respectively.

We use the matched-pairs t-test to examine whether order imbalance truncation trading strategy outperforms no truncation trading strategy. In Panel C of Table 9, we reject the null hypothesis. It implies that 90%-truncated trading strategy outperforms no-truncated one.

#### **4.7 Dynamic causality relationship in explaining the successful trading strategy**

To explore the reason why an order imbalance trading strategy earns a significant abnormal return, we employ a nested causality approach. In order to investigate a dynamic relationship between two variables, we impose the constraints in the upper panel of Table 2 on the VAR model. In Table 10, we present the empirical results of tests of hypotheses on the dynamic relationship in Table 3. Panel A presents results for the entire sample. In the entire sample, we show that a unidirectional relationship from returns to order imbalances is 11.43% of the sample firms for the entire sample, while a unidirectional relationship from order imbalances to returns is 12.86%. The percentage of firms that fall into the independent category is 20.00%. Moreover, 48.57% of firms exhibit a contemporaneous relationship between returns and order

imbalances. Finally, 7.14% of firms show a feedback relationship between returns and order imbalances. The percentage of firms carrying a unidirectional relationship from order imbalances to returns is larger than that from returns to order imbalances, suggesting that order imbalance is a better indicator for predicting future returns. It is consistent with many articles, which document that future daily returns could be predicted by daily order imbalances (Brown, Walsh, and Yuen (1997); Chordia et al. (2004)). In addition, the percentage of firms exhibiting a contemporaneous relationship is about seven times than that reflecting a feedback relationship, indicating that the interaction between returns and order imbalances on the current period is larger than that over the whole period.

In order to provide the evidence showing the impact on the relation between returns and order imbalances, in Panels B and C, we divide firms into three groups according to the firm size and turnover (daily trading volume/firm size). Then we test the multiple hypotheses of the relationship between returns and order imbalances. The results in Panel B indicate that the unidirectional relationship from order imbalances to returns is 13.04% in the small firm size quartile, while the corresponding number is 17.39% in the large firm size quartile during the entire sample period. The size-stratified results can be explained as follows. When the firm size is larger, the percentage of firms exhibiting a unidirectional relationship from order imbalances to returns is higher, indicating that order imbalance is a better indicator for predicting returns in large firm size quartile.

The results in Panel C indicate that the unidirectional relationship from order imbalances to returns is 17.39% in the small turnover quartile, while the corresponding number is 8.70% in the large turnover quartile during the entire sample period. The turnover-stratified results can be explained as follows. When the turnover is smaller, the percentage of firms exhibiting a unidirectional relationship from order

imbalances to returns is higher, indicating that order imbalance is a better indicator for predicting returns in small turnover quartile.

## **5. Conclusions**

In efficient market hypothesis, it was generally believed that securities markets were extremely efficient in reflecting information about individual stocks and stock market as a whole. The story is that when information arises, news spreads very quickly and is incorporated into the prices of securities simultaneously. However, markets do not reach efficiency within one second, convergence is a necessity. There must be some time interval, albeit very short, over which the actions of efficiency-creating traders remain incomplete. A central goal of this thesis is to present evidence about this important issue, the convergence to market efficiency.

We divided the market behavior into the following three steps: Order imbalances in the first instance arise from traders who demand immediacy for liquidity or informational needs. Order imbalance are positively auto-correlated, which suggests that traders are herding (Hirshleifer et al., 1994), or spreading their orders out over time (Kyle, 1985), or both. Second, market makers react to initial order imbalances by altering quotes away from fundamental value in an effort to control inventory. Finally, outside arbitrageurs intervene to add market-making capacity by conducting countervailing trades in the direction opposite to the initial order imbalances. This arbitrage activity takes at least a few minutes.

By selecting 70 samples of daily top losers from July 2006 to December 2006, we first examined the relations between returns and order imbalances. We found that both in OLS method and GARCH model the significance of order imbalance coefficients decreased with increasing time interval (5, 10 and 15-min), indicating that our findings were in agreement with the convergence process to market efficiency mentioned above.

Second, we used GARCH model to test the relations between order imbalances and volatilities. Again, the significant coefficients had a declining pattern which also supported the convergence to market efficiency.

Third, we ran the regression on small firm effect. The expected negative relation between order imbalance coefficients and market capitalizations was not achieved; as a consequence, the empirical results cannot make any conclusion on small firm effect.

Finally, we developed an imbalance-based trading strategy and made profit from these daily top losers. Our strategy was to short sell when seeing the first seller-initiated order imbalance and immediately buy back the underlying when the order imbalance transfer to buyer-initiated. We applied many methods in testing our strategy, such as using trading price or bid-ask price to evaluate the performance of the strategy, and selecting order imbalance with 0% or 90% truncation. All of them outperform buy and hold rate of return. Besides, the matched-pairs t-test showed that the average return of 90% truncated strategy was significant superior to that of no truncation in using bid-ask quote price.

Finally, according to our investigation of causal relationship between return and order imbalance, we find that order imbalance is a good indicator for predicting future returns. Moreover, order imbalance could be a better indicator for predicting returns in large firm size quartile.

## References

1. Aitken, M., Brown, P., Izan, H.Y. and Kua, A., 1995. "An Intraday Analysis of the Probability of Trading on the ASX at the Asking Price." *Australian Journal of Management*, 20, 116-154.
2. Barber, B. and Odean, T., 2000. "Trading is Hazardous to Your Health: the Common Stock Investment Performance of Individual Investors." *Journal of Finance*, 55, 773-806.
3. Benartzi, S. and Thaler, R., 2001. "Naive Diversification Strategies in Retirement Saving Plans." *American Economic Review*, 91, 79-98.
4. Brown, P., Walsh, D. M. and Yuen, 1997. "The Interaction between Order Imbalance and Stock Price." *Pacific-Basin Finance Journal*, 5:5, 539-557.
5. Busse, J. and Green, C., 2002. "Market Efficiency in Real Time." *Journal of Financial Economics*, 65, 415-437.
6. Chan, K. and Fong, W. M., 2000. "Trade Size, Order Imbalance, and the Volatility–Volume relation." *Journal of Financial Economics*, 57, 247–273.
7. Chordia, T., Roll, R. and Subrahmanyam, A., 2002. "Order Imbalance, Liquidity, and Market Returns." *Journal of Financial Economics*, 65, 111-130.
8. Chordia, T. and Subrahmanyam, A., 2004. "Order Imbalance and Individual Stock Returns: Theory and Evidence." *Journal of Financial Economics*, 72, 485-518.
9. Chordia, T., Roll, R. and Subrahmanyam, A., 2005. "Evidence on the Speed of Convergence to Market Efficiency." *Journal of Financial Economics*, 76, 271-292.
10. Chordia, T., Roll, R. and Subrahmanyam, A., 2008, "Liquidity and Market Efficiency." *Journal of Financial Economics*, 87, 249-268.
11. Cornell, B. and Roll, R., 1981. "Strategies for Pairwise Competitions in Markets and Organizations." *Bell Journal of Economics*, 12, 201-213.
12. Epps, T., 1979. "Comovements in Stock Prices in the Very Short Run." *Journal of the American Statistical Association*, 74, 291-298.
13. Fama, E., 1970. "Efficient Capital Markets: A Review of Theory and Empirical Work." *Journal of Finance*, 25,383-417.
14. Gallant, R., Rossi, P. and Tauchen, G., 1992. "Stock Prices and Volume." *Review of Financial Studies*, 5, 199-242.

15. Garbade, K. and Lieber, Z., 1977. "On the Independence of Transactions on the New York Stock Exchange." *Journal of Banking and Finance*, 1, 151-172.
16. Granger, C. and Morgenstern, O., 1963. "Spectral Analysis of New York Stock Market Prices." *Kyklos*, 16, 1-27.
17. Grossman, S., 1976. "On the Efficiency of Competitive Stock Markets Where Trades Have Diverse Information." *Journal of Finance*, 31(2), 573-585.
18. Grossman, S. and Stiglitz, J., 1980. "On the Impossibility of Informationally Efficient Markets." *American Economic Review*, 70, 393-408.
19. Harris, L., 1986. "Cross-Security Tests of the Mixture of Distributions Hypotheses." *Journal of Financial and Quantitative Analysis*, 21, 39-46.
20. Hirshleifer, D., Subrahmanyam, A. and Titman, S., 1994. "Security Analysis and Trading Patterns When Some Investors Receive Information before Others." *Journal of Finance*, 49, 1665-1698.
21. Karpoff, J., 1987. "The Relation between Price Changes and Trading Volume: A Survey." *Journal of Financial and Quantitative Analysis*, 22, 109-126.
22. Kyle, A., 1985. "Continuous Auctions and Insider Trading." *Econometrica*, 53, 1315-1335.
23. Lamoureux, C. and Lastrapes, W., 1990. "Heteroskedasticity in Stock Return Data: Volume versus GARCH Effects." *Journal of Finance*, 45, 221-229.
24. Lee, C. and Ready, M., 1991. "Inferring Trade Direction from Intraday Data." *Journal of Finance*, 46, 733-747.
25. Llorente, G., Michaely, R., Sarr, G. and Wang, J., 2002. "Dynamic Volume-Return Relation of Individual Stocks." *Review of Financial Studies*, 15, 1005-1047.
26. Morgan, I. G., 1976. "Stock Prices and Heteroskedasticity." *Journal of Business*, 49, 496-508.
27. Odean, T., 1999. "Do Investors Trade Too Much?" *American Economic Review*, 89, 1279-1298.
28. Osborne, M. F. M., 1959. Reply to "Comments on 'Brownian Motion in the Stock Market'". *Operations Research*, Vol. 7, No. 6, 807-811.
29. Patell, J. and Wolfson, M., 1984. "The Intra-day Speed of Adjustment of Stock Prices to Earnings and Dividend Announcements." *Journal of Financial Economics*, 13, 223-252.

## Table 1 Sample Information and statistics

### Panel A Descriptive statistics

	market cap (millions)	trade volume (thousands)	daily return
mean	135	5,311	-28.53%
median	48	1,524	-25.73%
standard deviation	220	12,724	9.63%
skewness	3.33	5.71	-0.90
kurtosis	13.28	38.35	0.42

### Panel B The distribution of market capitalization

market cap (million)	number of firms	%
0~100	42	60.00%
100~200	13	18.57%
200~300	8	11.43%
300~400	2	2.86%
400~500	1	1.43%
500~600	0	0.00%
600~700	1	1.43%
700~800	1	1.43%
800~900	1	1.43%
900~1000	0	0.00%
1000~1100	0	0.00%
1100~1200	0	0.00%
1200~	1	1.43%
total	70	100.00%

**Table 2 Hypotheses on the Dynamic Relationship of a Bivariate System**

The bivariate VAR model:  $\begin{bmatrix} \phi_{11}(L) & \phi_{12}(L) \\ \phi_{21}(L) & \phi_{22}(L) \end{bmatrix} \begin{bmatrix} x_{1t} \\ x_{2t} \end{bmatrix} = \begin{bmatrix} \varepsilon_{1t} \\ \varepsilon_{2t} \end{bmatrix}$  where  $x_{1t}$  and  $x_{2t}$  are mean

adjusted variables. The first and second moments of the error structure,  $\varepsilon_t = (\varepsilon_{1t}, \varepsilon_{2t})'$ , are that  $E(\varepsilon_t) = 0$ , and  $E(\varepsilon_t \varepsilon_{t+k}) = 0$  for  $k \neq 0$  and  $E(\varepsilon_t \varepsilon_{t+k}) = \Sigma$  for  $k=0$ , where

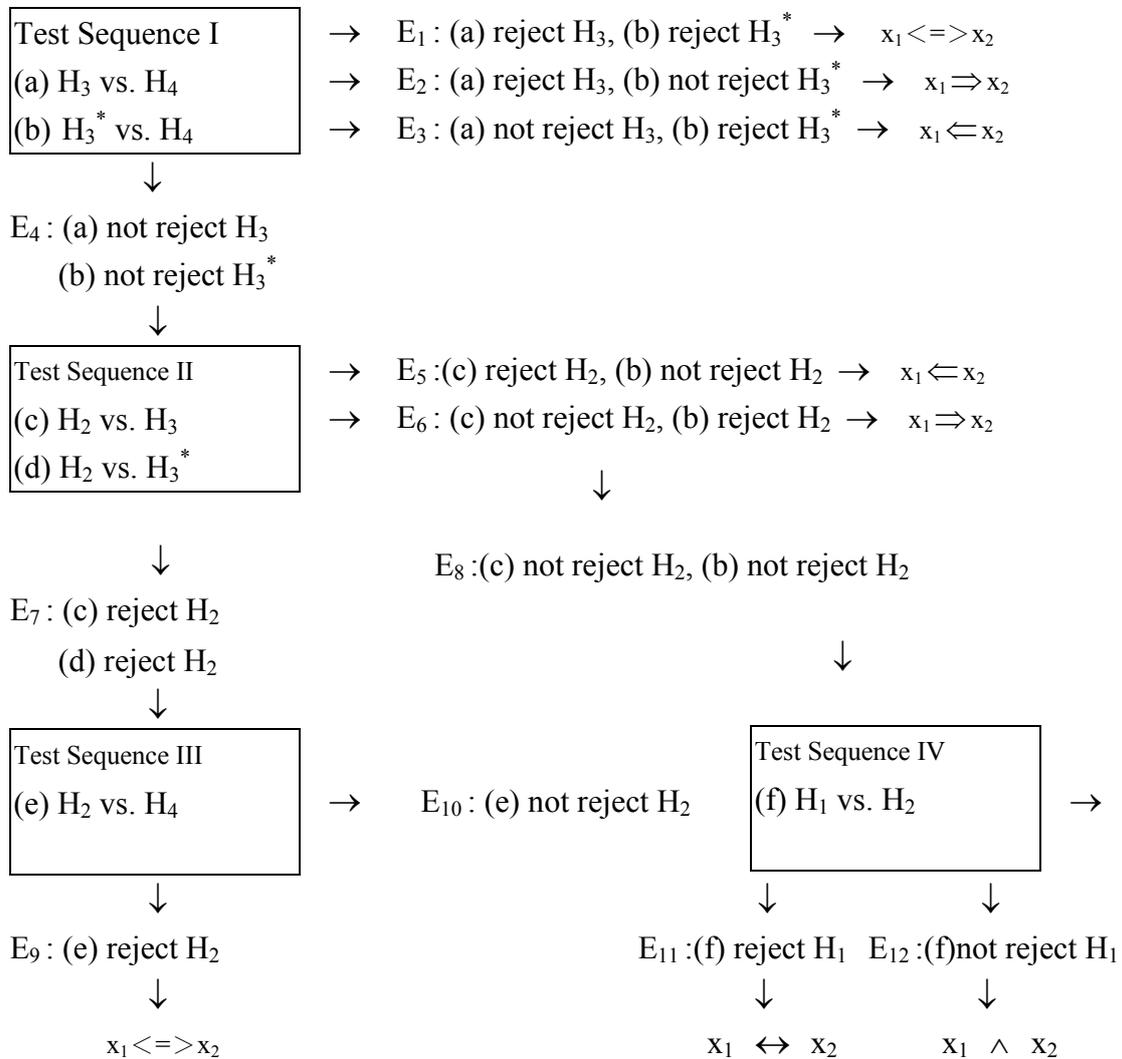
$$\Sigma = \begin{bmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{bmatrix}$$

The causal relationship are defined as follows:  $\wedge$  is independency;  $\langle - \rangle$  is contemporaneous relationship;  $\neq \rangle$  is negation of a unidirectional relationship;  $\langle = \rangle$  is feedback relationship;  $\neq \rangle \rangle$  is negation of a strong unidirectional relationship where  $\sigma_{12} = \sigma_{21} = 0$ ; and  $\langle \langle = \rangle \rangle$  is a strong feedback relationship where  $\sigma_{12} = \sigma_{21} = 0$

Hypotheses	The VAR test
$H_1 : x_1 \wedge x_2$	$\phi_{12}(L) = \phi_{21}(L) = 0$ , and $\sigma_{12} = \sigma_{21} = 0$
$H_2 : x_1 \langle - \rangle x_2$	$\phi_{12}(L) = \phi_{21}(L) = 0$
$H_3 : x_1 \neq \rangle x_2$	$\phi_{21}(L) = 0$
$H_3^* : x_2 \neq \rangle x_1$	$\phi_{12}(L) = 0$
$H_4 : x_1 \langle = \rangle x_2$	$\phi_{12}(L) * \phi_{21}(L) \neq 0$
$H_5 : x_1 \neq \rangle \rangle x_2$	$\phi_{21}(L) = 0$ , and $\sigma_{12} = \sigma_{21} = 0$
$H_6 : x_2 \neq \rangle \rangle x_1$	$\phi_{12}(L) = 0$ , and $\sigma_{12} = \sigma_{21} = 0$
$H_7 : x_1 \langle \langle = \rangle \rangle x_2$	$\phi_{12}(L) * \phi_{21}(L) \neq 0$ , and $\sigma_{12} = \sigma_{21} = 0$

### Table 3 Test Flow Chart of a Multiple Hypothesis Testing Procedure

Five groups of dynamic relationship are identified: independency ( $\wedge$ ), the contemporaneous relationship ( $\leftrightarrow$ ), unidirectional relationship ( $\Rightarrow$  or  $\Leftarrow$ ) and feedback relationship ( $\Leftrightarrow$ ). To determine a specific causal relationship, we use a systematic multiple hypotheses testing method. Unlike the traditional pairwise hypothesis testing, this testing method avoids the potential bias induced by restricting the causal relationship to a single alternative hypothesis. In implementing this method, we need to employ results of several pairwise hypothesis tests. For instance, in order to conclude that  $x_1 \Rightarrow x_2$ , we need to establish that  $x_1 \neq x_2$  and to reject that  $x_1 \neq x_2$ . To conclude that  $x_1 \Leftarrow x_2$ , we need to establish that  $x_1 \neq x_2$  as well as  $x_1 \neq x_2$  and also to reject  $x_1 \wedge x_2$ . In other words, it is necessary to examine all five hypotheses in a systematic way before a conclusion of dynamic relationship can be drawn.



**Table 4 Significance test results of unconditional order imbalance regressions - lagged 1 through lagged 5**

$$R_t = \alpha + \beta_1 \times OI_{t-1} + \beta_2 \times OI_{t-2} + \beta_3 \times OI_{t-3} + \beta_4 \times OI_{t-4} + \beta_5 \times OI_{t-5} + \varepsilon_t$$

Where  $R_t$  is the stock return in period t, defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_{t-i}, i=1,2,3,4,5$  are lagged order imbalance at time t-1,t-2, t-3, t-4, t-5 of the stock

**Panel A Significance test results of 10% significance level**

$\alpha=10\%$	return interval(in numbers)						return interval(%)											
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	26	26	1	23	24	1	19	20	0%	37%	37%	1%	33%	34%	1%	28%	29%
$OI_{t-1}$	10	6	16	7	7	14	8	7	15	14%	9%	23%	10%	10%	20%	12%	10%	22%
$OI_{t-2}$	8	9	17	8	8	16	7	8	15	11%	13%	24%	11%	11%	23%	10%	12%	22%
$OI_{t-3}$	4	3	7	5	6	11	3	6	9	6%	4%	10%	7%	9%	16%	4%	9%	13%
$OI_{t-4}$	10	6	16	4	7	11	2	5	7	14%	9%	23%	6%	10%	16%	3%	7%	10%
$OI_{t-5}$	5	8	13	3	5	8	5	6	11	7%	11%	19%	4%	7%	11%	7%	9%	16%

**Panel B Significance test results of 5% significance level**

$\alpha=5\%$	return interval(in numbers)						return interval(%)											
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	19	19	1	14	15	1	8	9	0%	27%	27%	1%	20%	21%	1%	12%	13%
$OI_{t-1}$	8	5	13	6	6	12	6	4	10	11%	7%	19%	9%	9%	17%	9%	6%	14%
$OI_{t-2}$	7	8	15	5	8	13	3	5	8	10%	11%	21%	7%	11%	19%	4%	7%	12%
$OI_{t-3}$	3	2	5	4	5	9	1	4	5	4%	3%	7%	6%	7%	13%	1%	6%	7%
$OI_{t-4}$	6	3	9	2	7	9	1	4	5	9%	4%	13%	3%	10%	13%	1%	6%	7%
$OI_{t-5}$	3	6	9	1	2	3	2	5	7	4%	9%	13%	1%	3%	4%	3%	7%	10%

**Panel C Significance test results of 1% significance level**

$\alpha=1\%$	return interval(in numbers)						return interval(%)											
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	4	4	0	6	6	0	4	4	0%	6%	6%	0%	9%	9%	0%	6%	6%
$OI_{t-1}$	6	2	8	4	3	7	2	2	4	9%	3%	11%	6%	4%	10%	3%	3%	6%
$OI_{t-2}$	4	4	8	2	2	4	3	2	5	6%	6%	11%	3%	3%	6%	4%	3%	7%
$OI_{t-3}$	1	1	2	2	1	3	0	2	2	1%	1%	3%	3%	1%	4%	0%	3%	3%
$OI_{t-4}$	4	2	6	0	3	3	0	1	1	6%	3%	9%	0%	4%	4%	0%	1%	1%
$OI_{t-5}$	0	2	2	1	1	2	0	3	3	0%	3%	3%	1%	1%	3%	0%	4%	4%

**Table 5 Significance test results of conditional order imbalance regressions - lagged 0 through lagged 4**

$$R_t = \alpha + \beta_1 \times OI_t + \beta_2 \times OI_{t-1} + \beta_3 \times OI_{t-2} + \beta_4 \times OI_{t-3} + \beta_5 \times OI_{t-4} + \varepsilon_t$$

Where  $R_t$  is the stock return in period  $t$ , defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_{t-i}$ , are order imbalance at time  $t, t-1, t-2, t-3, t-4$  of the stock

**Panel A Significance test results of 10% significance level**

$\alpha=10\%$	return interval(in numbers)									return interval(%)								
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	20	20	1	20	21	1	16	17	0%	29%	29%	1%	29%	30%	1%	23%	25%
$OI_t$	47	3	50	38	4	42	32	1	33	67%	4%	71%	54%	6%	60%	46%	1%	48%
$OI_{t-1}$	9	10	19	7	8	15	4	10	14	13%	14%	27%	10%	11%	21%	6%	14%	20%
$OI_{t-2}$	7	11	18	5	9	14	6	7	13	10%	16%	26%	7%	13%	20%	9%	10%	19%
$OI_{t-3}$	4	6	10	5	10	15	4	7	11	6%	9%	14%	7%	14%	21%	6%	10%	16%
$OI_{t-4}$	7	4	11	3	7	10	3	4	7	10%	6%	16%	4%	10%	14%	4%	6%	10%

**Panel B Significance test results of 5% significance level**

$\alpha=5\%$	return interval(in numbers)									return interval(%)								
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	15	15	0	14	14	0	11	11	0%	21%	21%	0%	20%	20%	0%	16%	16%
$OI_t$	44	2	46	33	3	36	28	1	29	63%	3%	66%	47%	4%	51%	41%	1%	42%
$OI_{t-1}$	7	6	13	5	6	11	4	9	13	10%	9%	19%	7%	9%	16%	6%	13%	19%
$OI_{t-2}$	7	7	14	3	8	11	4	6	10	10%	10%	20%	4%	11%	16%	6%	9%	14%
$OI_{t-3}$	3	4	7	4	7	11	3	6	9	4%	6%	10%	6%	10%	16%	4%	9%	13%
$OI_{t-4}$	6	3	9	1	6	7	2	2	4	9%	4%	13%	1%	9%	10%	3%	3%	6%

**Panel C Significance test results of 1% significance level**

$\alpha=1\%$	return interval(in numbers)									return interval(%)								
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins		
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
intercept	0	4	4	0	2	2	0	3	3	0%	6%	6%	0%	3%	3%	0%	4%	4%
$OI_t$	37	1	38	27	3	30	21	1	22	53%	1%	54%	39%	4%	43%	30%	1%	32%
$OI_{t-1}$	5	3	8	4	3	7	2	5	7	7%	4%	11%	6%	4%	10%	3%	7%	10%
$OI_{t-2}$	5	5	10	1	2	3	4	2	6	7%	7%	14%	1%	3%	4%	6%	3%	9%
$OI_{t-3}$	2	3	5	3	5	8	3	1	4	3%	4%	7%	4%	7%	11%	4%	1%	6%
$OI_{t-4}$	2	1	3	0	2	2	0	1	1	3%	1%	4%	0%	3%	3%	0%	1%	1%

**Table 6 The significant test of contemporaneous return - order imbalance relation in GARCH (1,1)**

$$R_t = \alpha + \beta \times OI_t + \varepsilon_t \quad \varepsilon_t \mid \Omega_{t-1} \sim N(0, h_t)$$

$$h_t = A_1 + B_1 h_{t-1} + C_1 \varepsilon_{t-1}^2$$

where  $R_t$  is the return in period  $t$ , defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_t$  is the explanatory variable, order imbalance

$\beta$  is the coefficient of the impact of order imbalance on stock returns

$\varepsilon_t$  means the residual of the stock return in period  $t$

$h_t$  is the conditional variance in the period  $t$

$\Omega_{t-1}$  is the information set in period  $t-1$

	return interval(in numbers)									return interval(%)											
	5 mins			10 mins			15 mins			5 mins			10 mins			15 mins					
	OI (in numbers)			OI (in numbers)			OI (in numbers)			OI (%)			OI (%)			OI (%)					
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
		46	24	70	44	26	70	45	25	70	66%	34%	100%	63%	37%	100%	64%	36%	100%		
significant level	significance (in numbers)			significance (in numbers)			significance (in numbers)			significance (%)			significance (%)			significance (%)					
	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total	+	-	total
$\alpha=10\%$	32	11	43	29	8	37	20	5	25	46%	16%	61%	41%	11%	53%	29%	7%	36%			
$\alpha=5\%$	32	8	40	28	6	34	15	4	19	46%	11%	57%	40%	9%	49%	21%	6%	27%			
$\alpha=1\%$	31	4	35	22	6	28	11	3	14	44%	6%	50%	31%	9%	40%	16%	4%	20%			

**Table 7 The significant test of contemporaneous volatility - order imbalance relation in GARCH (1,1)**

$$R_t = \alpha + \varepsilon_t \quad \varepsilon_t \mid \Omega_{t-1} \sim N(0, h_t)$$

$$h_t = A_1 + B_1 h_{t-1} + C_1 \varepsilon_{t-1}^2 + D_1 OI_t$$

where  $R_t$  is the return in period t, defined as  $(P_t - P_{t-1})/P_{t-1}$

$OI_t$  is the explanatory variable, order imbalance

$\varepsilon_t$  means the residual of the stock return in period t

$h_t$  is the conditional variance in the period t

$\Omega_{t-1}$  is the information set in period t-1

	return interval			return interval		
	5 mins	10 mins	15 mins	5 mins	10 mins	15 mins
	OI	OI	OI	OI	OI	OI
	(in numbers)	(in numbers)	(in numbers)	(%)	(%)	(%)
	+ - total	+ - total	+ - total	+ - total	+ - total	+ - total
	31 35 66	28 38 66	34 32 66	47% 53% 100%	42% 58% 100%	52% 48% 100%
significant level	significance	significance	significance	significance	significance	significance
	(in numbers)	(in numbers)	(in numbers)	(%)	(%)	(%)
	+ - total	+ - total	+ - total	+ - total	+ - total	+ - total
$\alpha=10\%$	8 13 21	7 4 11	6 4 10	12% 20% 32%	11% 6% 17%	9% 6% 15%
$\alpha=5\%$	8 8 16	4 4 8	4 1 5	12% 12% 24%	6% 6% 12%	6% 2% 8%
$\alpha=1\%$	6 7 13	3 3 6	1 1 2	9% 11% 20%	5% 5% 9%	2% 2% 3%

**Table 8 Empirical results of small firm effect tests**

a.  $\alpha_i = \theta_0 + \theta_1(\text{Market Cap})_i + \varepsilon_i$

Where  $\alpha_i$  is the coefficients of the order imbalance of each stock  
 $\theta_0$  is the intercept  
 $\theta_1$  is the coefficient of the market cap of each stock  
 $\varepsilon_i$  is the residual of the stock

b.  $\alpha_i = \theta_0 + \theta_1 \ln(\text{Market Cap})_i + \varepsilon_i$

Where  $\alpha_i$  is the coefficients of the order imbalance of each stock  
 $\theta_0$  is the intercept  
 $\theta_1$  is the coefficient of the market cap of each stock  
 $\varepsilon_i$  is the residual of the stock

**Panel A Results of small firm effect test using the OI coefficients from GARCH method**

GARCH		5 mins	10 mins	15 mins
CAP	$\theta_1$	1.55E-14	-2.7E-16	5.59E-15
	t-value	(0.2786)	(-0.0049)	(0.1222)
	R square	0.0011	0.0000	0.0002
ln(CAP)	$\theta_1$	2.86E-06	-5.4E-06	2.6E-06
	t-value	(0.3714)	(-0.7223)	(0.4128)
	R square	0.0020	0.0076	0.0025

**Panel B Results of small firm effect test using the OI coefficients from OLS method**

OLS		5 mins	10 mins	15 mins
CAP	$\theta_1$	-6.1E-16	-4.7E-16	-5.7E-16
	t-value	(-1.4269)	(-0.8746)	(-1.1650)
	R square	0.0291	0.0111	0.0199
ln(CAP)	$\theta_1$	-7.6E-08	-2.4E-08	-4.1E-08
	t-value	(-1.2874)	(-0.3193)	(-0.6111)
	R square	0.0238	0.0015	0.0055

**Table 9 Results of return from speculative trading strategy**

**Panel A. Daily return and the return from strategy under 0% and 90% OI truncated in each sample stocks– using trading price**

stock	daily return	5 mins		10 mins		15 mins	
		no truncated	90% truncated	no truncated	90% truncated	no truncated	90% truncated
Average return	-28.53%	9.16%	5.86%	9.90%	1.14%	10.35%	4.14%

**Panel B. Daily return and the return from strategy under 0% and 90% OI truncated in each sample stocks– using bid/ask price**

stock	daily return	5 mins		10 mins		15 mins	
		no truncated	90% truncated	no truncated	90% truncated	no truncated	90% truncated
Average return	-28.53%	-24.91%	-1.30%	-9.93%	-5.04%	-6.47%	-1.13%

**Panel C. Significant test on no truncated and 90% truncated speculative trading strategies.**

Null hypothesis	$H_0: \mu_1 \geq \mu_2$
Alternative hypothesis	$H_1: \mu_1 < \mu_2$
$\alpha$	5%
T value	-5.71
P value	0.00000
Degrees of Freedom	120

**Table 10 Dynamic Nested Causality Relationship between Returns and Order Imbalances (in percentage)**

The causal relationship are defined as follows:  $\wedge$  is independency;  $\langle - \rangle$  is contemporaneous relationship;  $\neq \rangle$  is negation of a unidirectional relationship;  $\langle = \rangle$  is feedback relationship;  $\neq \rangle \rangle$  is negation of a strong unidirectional relationship where  $\sigma_{12} = \sigma_{21} = 0$ ; and  $\langle \langle = \rangle \rangle$  is a strong feedback relationship where  $\sigma_{12} = \sigma_{21} = 0$ .

	$x_1 \wedge x_2$	$x_1 \langle - \rangle x_2$	$x_1 \Rightarrow x_2$	$x_1 \Leftarrow x_2$	$x_1 \langle = \rangle x_2$
<b>Panel A: All Size</b>					
All Trade Size	20.00	48.57	11.43	12.86	7.14
<b>Panel B: Firm Size</b>					
Small Firm Size	21.74	43.48	13.04	13.04	8.70
Medium Firm Size	12.50	54.17	16.67	8.33	8.33
Large Firm Size	26.09	47.83	4.35	17.39	4.35
<b>Panel C: Turnover</b>					
Small Turnover	17.39	56.52	8.70	17.39	0.00
Medium Turnover	20.83	41.67	16.67	12.50	8.33
Large Turnover	21.74	47.83	8.70	8.70	13.04